

Dsolv Manual

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1 DSOLV Functions

This section is a collection of functions to solve regular holonomic systems in terms of series. Algorithms are explained in the book [SST]. You can load this package by the command `load("dsolv.rr")` \$ This package requires `Diff` and `dmodule`.

To use the functions of the package `dsolv` in OpenXM/Risa/Asir, executing the command `load("dsolv.rr")` \$ is necessary at first.

This package uses `ox_sm1`, so the variables you can use is as same as those you can use in the package `sm1`.

1.1 Functions

1.1.1 dsolv_dual

`dsolv_dual(f, v)`
 :: Grobner dual of f .

return List

f, v List

- It returns the Grobner dual of f in the ring of polynomials with variables v .
- The ideal generated by f must be primary to the maximal ideal generated by v . If it is not primary to the maximal ideal, then this function falls into an infinite loop.

Algorithm: This is an implementation of Algorithm 2.3.14 of the book [SST]. If we replace variables x, y, \dots in the output by $\log(x), \log(y), \dots$, then these polynomials in \log are solutions of the system of differential equations $f_-(x \rightarrow x \cdot dx, y \rightarrow y \cdot dy, \dots)$.

```
[435] dsolv_dual([y-x^2,y+x^2],[x,y]);
[x,1]
[436] dsolv_act(y*dy-sm1.mul(x*dx,x*dx,[x,y]),log(x),[x,y]);
0
[437] dsolv_act(y*dy+sm1.mul(x*dx,x*dx,[x,y]),log(x),[x,y]);
0

[439] primadec([y^2-x^3,x^2*y^2],[x,y]);
[[[y^2-x^3,y^4,x^2*y^2],[y,x]]]
[440] dsolv_dual([y^2-x^3,x^2*y^2],[x,y]);
[x*y^3+1/4*x^4*y, x^2*y, x*y^2+1/12*x^4, y^3+x^3*y,
x^2, x*y, y^2+1/3*x^3, x, y, 1]

[441] dsolv_test_dual();
Output is omitted.
```

1.1.2 dsolv_starting_term

`dsolv_starting_term(f, v, w)`

:: Find the starting term of the solutions of the regular holonomic system f to the direction w .

`return` List

f, v, w List

- Find the starting term of the solutions of the regular holonomic system f to the direction w .
- The return value is of the form $[[e1, e2, \dots], [s1, s2, \dots]]$ where $e1$ is an exponent vector and $s1$ is the corresponding solution set, and so on.
- If you set `Dsolv_message_starting_term` to 1, then this function outputs messages during the computation.

Algorithm: Saito, Sturmfels, Takayama, Grobner Deformations of Hypergeometric Differential Equations ([SST]), Chapter 2.

```
[1076] F = sm1.gkz( [ [[1,1,1,1,1],[1,1,0,-1,0],[0,1,1,-1,0]], [1,0,0]]);
[[x5*dx5+x4*dx4+x3*dx3+x2*dx2+x1*dx1-1,-x4*dx4+x2*dx2+x1*dx1,
-x4*dx4+x3*dx3+x2*dx2,
-dx2*dx5+dx1*dx3,dx5^2-dx2*dx4],[x1,x2,x3,x4,x5]]
[1077] A= dsolv_starting_term(F[0],F[1],[1,1,1,1,0])$
Computing the initial ideal.
Done.
Computing a primary ideal decomposition.
Primary ideal decomposition of the initial Frobenius ideal
to the direction [1,1,1,1,0] is
[[[x5+2*x4+x3-1,x5+3*x4-x2-1,x5+2*x4+x1-1,3*x5^2+(8*x4-6)*x5-8*x4+3,
x5^2-2*x5-8*x4^2+1,x5^3-3*x5^2+3*x5-1],
[x5-1,x4,x3,x2,x1]]]

----- root is [ 0 0 0 0 1 ]
----- dual system is
[x5^2+(-3/4*x4-1/2*x3-1/4*x2-1/2*x1)*x5+1/8*x4^2
+(1/4*x3+1/4*x1)*x4+1/4*x2*x3-1/8*x2^2+1/4*x1*x2,
x4-2*x3+3*x2-2*x1,x5-x3+x2-x1,1]

[1078] A[0];
[[ 0 0 0 0 1 ]]
[1079] map(fctr,A[1][0]);
[[[1/8,1],[x5,1],[log(x2)+log(x4)-2*log(x5),1],
[2*log(x1)-log(x2)+2*log(x3)+log(x4)-4*log(x5),1]],
[[1,1],[x5,1],[-2*log(x1)+3*log(x2)-2*log(x3)+log(x4),1]],
[[1,1],[x5,1],[-log(x1)+log(x2)-log(x3)+log(x5),1]],
[[1,1],[x5,1]]]
```

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