

@comment *OpenXM : OpenXM/src/asir-contrib/packages/doc/todo_parametrize/todo_parametrize-
ja.texi, v1.22017/03/3006 : 16 : 37takayamaExp* @comment Copyright (c) 2005, Shuhei Todo, @comment
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Risa/Asir

1.0
2004 8

by Shuhei Todo

1

1.1

- 2
 -
 - neighborhood graph tree
 -
 - (adjoint curves)
 -
 -
- x, y, z

1.2 Notation

- $[x, y, z] \quad (x:y:z)_{z=0} \quad z=1$
- $Q \quad \overline{Q}$

1.3

1.3.1 intersect

`intersect(F, G)`
 $:: 2F=0, G=0 .$

return

$F \ G \quad x, y, z$

- $2F=0, G=0 \ [x, y, z]$
- F, G

```

[1] intersect(y^2-x*z, (x^2+y^2)^3-4*x^2*y^2*z^2);
[[0,0,1],[#4],[#5],1]]
[2] defpoly(alg(4));
t#4^3+3*t#4^2+3*t#4-3
[3] defpoly(alg(5));
t#5^2-t#4
[4] intersect(x^2-y^2, x^3+y*x^2+(y^2-z^2)*x+y^3-z^2*y);
***two curve have common components***

```

1.3.2 sing

`sing(F)` $:: F=0 .$

return

F x,y,z

- $F=0$ $[x,y,z]$ $F_x(x,y,z) = F_y(x,y,z) = F_z(x,y,z) = 0$

- F

```
[1] sing(16*x^6-24*z^2*x^4+9*z^4*x^2+4*z^2*y^4-4*z^4*y^2);
[[0,0,1],[(#4),0,1],[1/2,(#3),1],[-1/2,(#3),1],[0,1,0]]
[2] defpoly(alg(3));
2*t#3^2-1
[3] defpoly(alg(4));
4*t#4^2-3
[4] sing((x-y)*(y^2-x*z));
[[1,1,1],[0,0,1]]
[5] sing((x-y)^2*(y^2-x*z));
***Argument has multiple divisor***
```

Section 1.3.3 [nbh], page 2, Section 1.4.4 [multia], page 5,

1.3.3 nbh

$\text{nbh}(F)$:: $F=0$ neighborhood graph

return

F x,y,z

- $F=0$ neighborhood graph neighborhood graph tree

```
[ , , [, (=1)(=-1)], [("terminal")] ]
```

```
[ , [, (=1)(=-1)], [("terminal")] ]
```

=1

- neighborhood graph

```
[1] F=x^6+3*y^2*x^4+(3*y^4-4*z^2*y^2)*x^2+y^6;
```

```
x^6+3*y^2*x^4+(3*y^4-4*z^2*y^2)*x^2+y^6
```

```
[2] sing(F);
```

```
[[0,0,1],[(#0),1,0]]
```

```
[3] nbh(F);
```

```
[ 1 [0,0,1] [4,-1] [[ 1 [2,1] [terminal] ],[ 1 [2,1] [terminal] ]] ]
```

```
[ 2 [(#0),1,0] [2,-1] [[ 1 [1,1] [terminal] ]] ]
```

```
[0,0,1] 4 22 [(#0),1,0]
```

- F

Section 1.3.2 [sing], page 1,

1.3.4 genus

$\text{genus}(F)$:: $F=0$.

return 0

F x,y,z

- $F=0$

- $F \overline{Q}[x, y, z] \overline{Q}[x, y, z]$
 - [1] genus($x^6+3y^2x^4+(3y^4-4z^2y^2)x^2+y^6$);
0
 - [2] genus($y^2z-x^3-z^3$);
1
 - [3] genus($x^2+y^2+z^2-xy-yz-zx$);
-1
 - [4] fctr($x^2+y^2+z^2-xy-yz-zx$);
[[1, 1], [$x^2+(-y-z)x+y^2-z*y+z^2$, 1]]
 - [5] irr_conic($x^2+y^2+z^2-xy-yz-zx$);
reducible

Section 1.4.5 [irr_conic], page 6,

1.3.5 adjoint1,adjoint2

adjoint1(F)

adjoint2(F)

:: $F=0$ n-1, n-2 (adjoint curve) (n=deg(F))

return x,y,z

F x,y,z

- n-2 $G=0$ F=0 r r-1 $G=0$ F=0 n-2 (adjoint curve) n-1 $G_0 = 0, G_1 = 0, \dots, G_{n-2} = 0$ n-2
 $c_0G_0 + c_1G_1 + \dots + c_{n-2}G_{n-2}$ (c_i) adjoint2(F) n-1 n-1 n-1 2n-1 n-1 adjoint1(F)
-
- F

```
[1] adjoint2(x^6+3*y^2*x^4+(3*y^4-4*z^2*y^2)*x^2+y^6);
[c2,c3,c4,c6,c7] 5
(c2-c4)*x^4+c3*y*x^3+(c2*y^2+c6*z*y)*x^2+(c3*y^3+c7*z*y^2)*x+c4*y^4
[2] adjoint1(F);
[c1,c7,c11,c12,c13,c15,c16,c17,c18,c19,c20] 11
(c1*y+(c11-c15+c18-c20)*z)*x^4+(c13*y^2+c7*z*y+c11*z^2)*x^3+(c17*z*y^2+c12*z^2*y
+c15*z^3)*x^2+(c13*z^2*y^2+c16*z^3*y+c18*z^4)*x+c17*z^3*y^2+c19*z^4*y+c20*z^5
```

Section 1.4.7 [restriction], page 6,

1.3.6 intpt

intpt(F) :: $F=0$ [x,y,z] no integer solution

return no integer solution.

F x,y,z

- $F=0$ (affine) [x,y,z] x,y, z no integer solution
- LegendreF

```
[1] intpt(22*x^2-10*y^2+z^2+5*x*y+13*y*x-z*x);
[71,-121,473]
[2] intpt(22*x^2-10*y^2+z^2+5*x*y+12*y*x-z*x);
no integer solution
```

1.3.7 parametrize

```

parametrize(F)
  :: F=0

return

F      x,y,z
• F=0  P(t),Q(t),R(t)      x,y,zS(x,y,z),T(x,y,z)(x:y:z)=(P(t):Q(t):R(t)),
  t=T(x,y,z)/S(x,y,z)      parametrize(F)      [P(t),Q(t),R(t),T(x,y,z)/S(x,y,z)]
  GCD(P(t),Q(t),R(t))=1 P(t),Q(t),R(t)

• F Q[x,y,z] 0
  [1] parametrize(x^4+(2*y^2-z^2)*x^2+y^4+z^2*y^2);
  [-t^3-t,t^3-t,t^4+1,(-x^2-y^2)/(z*x+z*y)]
  [2] parametrize((x^2+y^2)^3-4*x^2*y^2*z^2);
  heuristic2 failed...
  heuristic3 succeed
  [32256*t^6-133120*t^5-129024*t^4+1064960*t^3-516096*t^2
  -2129920*t+2064384,-127008*t^6+1048320*t^5-2671232*t^4
  +10684928*t^2-16773120*t+8128512,274625*t^6-3194100*t^5
  +15678780*t^4-41555808*t^3+62715120*t^2-51105600*t+17576000,
  (-126*x^4+1040*y*x^3-382*y^2*x^2+1040*y^3*x-256*y^4)
  /(-65*x^4+520*y*x^3+(-65*y^2-32*z*y)*x^2+(520*y^3+256*z*y^2)*x)]
  [3] parametrize(22*x^2-10*y^2+z^2+5*x*y+12*y*x-z*x);
  [(220*#6-10)*t^2+(-22*#6+1),(374*#6-17)*t^2+(-22*#6-43)*t,
  (220*#6+210)*t^2+(-374*#6+17)*t+22,(-y)/((22*#6-1)*x+z)]

Section 1.3.4 [genus], page 2,

```

1.4

1.4.1 tdeg

```

tdeg(Poly)
  :: Poly

return 0

Poly
• Poly
  [1] tdeg(u^3+v^3-x*y*z*w);
  4
  [956] tdeg((x^3+y^2+z)*(a^2+b+1));
  5

```

1.4.2 homzation

```

homzation(AF)
  :: x,yx,y,z

return x,y,z

```

F *x,y*

- *x,yx,y,zx,y*

```
[1] homzation((x^2+4*x^3+6*x^4)-4*x^4*y
+(-2*x-4*x^2-2*x^3)*y^2+y^4);
(-4*y+6*z)*x^4+(-2*y^2+4*z^2)*x^3
+(-4*z*y^2+z^3)*x^2-2*z^2*y^2*x+z*y^4
[958] homzation(u*v+1);
Input must be polynomial of variable x,y
```

1.4.3 random_line

```
random_line(Pt,B[,Seed])
:: Pt(=[x,y,z])
```

return *x,y,z*

Pt

B

Seed

- *Pt(=[x,y,z]) -BB*
- *Seedrandom([Seed])*

```
[1] random_line([0,0,1],1);
x-8*y
```

1.4.4 multia

```
multia(F,Pt)
:: F=0 Pt(=[x,y,z])
```

return 0

F *x,y,z*

Pt

- *F=0 Pt(=[x,y,z]) FN Pt 0NF=0Pt*

```
[1] multia((4*y^2+4*z^2)*x^4+8*z^3*x^3+8*z^2*y^2*x^2-8*z^5*x+
4*z^4*y^2-4*z^6,[0,0,1]);
0
[2] multia((4*y^2+4*z^2)*x^4+8*z^3*x^3+8*z^2*y^2*x^2-8*z^5*x+
4*z^4*y^2-4*z^6,[0,1,0]);
4
[3] multia((4*y^2+4*z^2)*x^4+8*z^3*x^3+8*z^2*y^2*x^2-8*z^5*x+
4*z^4*y^2-4*z^6,[1,0,0]);
2
```

1.4.5 irr_conic

```
irr_conic(F)
      ::  $F \overline{Q}[x, y, z]$ 

return

F      x,y,z
•  $F \overline{Q}[x, y, z]$  irreducible
  [1] irr_conic( $x^2+y^2+z^2-x*y-y*z-z*x$ );
      reducible
  [2] fctr( $x^2+y^2+z^2-x*y-y*z-z*x$ );
      [[1,1], [ $x^2+(-y-z)*x+y^2-z*y+z^2$ ,1]]
```

1.4.6 lissajou

```
lissajou(M,N)
      ::  $x = \sin(M\theta), y = \cos(N\theta)$ 

return      x,y,z

M N
•  $x = \sin(M\theta), y = \cos(N\theta)$  x,y,z
  [984] lissajou(3,4);
       $64*x^8-128*z^2*x^6+80*z^4*x^4-16*z^6*x^2+16*z^2*y^6$ 
       $-24*z^4*y^4+9*z^6*y^2$ 
  [985] lissajou(2,7);
       $4096*x^{14}-14336*z^2*x^{12}+19712*z^4*x^{10}-13440*z^6*x^8$ 
       $+4704*z^8*x^6-784*z^{10}*x^4+49*z^{12}*x^2+4*z^{10}*y^4-4*z^{12}*y^2$ 
```

1.4.7 restriction

```
restriction(A,List)
      ::

return      x,y,z

A      adjoint1,adjoint2 x,y,z

List      [x,y,z]
• adjoint1,adjoint2 List Q
• Listintersectsing
      ⟨undefined⟩ [adjoint1], page ⟨undefined⟩,
```


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