

Package ‘hgmFB’

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Type Package

Depends R (>= 2.6.0)

Title Fisher-Bingham Distribution by HGM

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Description This package evaluates the normalizing constant for the Fisher-Bingham distributions and solves MLE problems by utilizing the holonomic gradient method (HGM)

License GPL-2

LazyLoad yes

URL <http://www.openxm.org>

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hgmFB-package	<i>HGM</i>
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Description

This package evaluates the normalizing constant for the Fisher-Bingham distributions and solves MLE problems by utilizing the holonomic gradient method.

Details

Package: hgm_fb
 Type: Package
 License: GPL-2
 LazyLoad: yes

This package evaluates the normalizing constant for the Fisher-Bingham distributions and solves MLE problems by utilizing the holonomic gradient method. The HGM and HGD are proposed in the paper below. This method based on the fact that a broad class of normalizing constants of unnormalized probability distributions belongs to the class of holonomic functions, which are solutions of holonomic systems of linear partial differential equations.

References

- N3OST2 Hiromasa Nakayama, Kenta Nishiyama, Masayuki Noro, Katsuyoshi Ohara, Tomonari Sei, Nobuki Takayama, Akimichi Takemura, Holonomic Gradient Descent and its Application to Fisher-Bingham Integral, *Advances in Applied Mathematics* 47 (2011), 639–658, <http://dx.doi.org/10.1016/j.aam.2011.03.001>
- dojo Edited by T.Hibi, *Groebner Bases: Statistics and Software Systems*, Springer, 2013, <http://dx.doi.org/10.1007/978-4-431-54574-3>
- <http://www.openxm.org>

See Also

[hgm.z.mleFBByOptim](#),

hgm.z.mleFBByOptim *MLE of Fisher-Bingham distribution by optim and HGM.*

Description

It makes the maximal likelihood estimate (MLE) for the Fisher-Bingham distribution on S^d .

Usage

```
hgm.z.mleFBByOptim(d=0, ss=NULL, data=NULL, start=NULL, lb=NULL, ub=NULL, bigValue=10000)
```

Arguments

d	The dimension of the sphere
ss	Sufficient statistics
data	The argument data is a set of data on the d-dimensional sphere. Its format is an n by (d+1) matrix where n is the number of data. When data is given, ss must be NULL and ss is calculated from data by <code>hgm.ssFB(data)</code> .
start	Starting point for the function optim. The default value is a random vector.

lb	An array of length $sslen = (d+1)*(d+2)/2 + (d+1)$, each of which is the lower bound of the parameter. The default value is -100.
ub	An array of length $sslen = (d+1)*(d+2)/2 + (d+1)$, each of which is the upper bound of the parameter. The default value is 100.
bigValue	It is used as a value wall to avoid that the evaluation point is out of the search domain defined by lb and ub.

Details

It solves the MLE for the Fisher-Bingham distribution. The normalizing constant is evaluated by hgm_ko_ncfb (external program, which should in the path). The function `optim` is used for the optimization. The output is used as a starting point for the holonomic gradient method. See `nk_fb_gen_c.rr` of <http://www.math.kobe-u.ac.jp/Asir>. This function generates temporary work files whose names start with tmp. `data <- read.table(fileName,sep=",")` can be used to read CSV data from a file.

Value

The output format is that of the function `optim()`.

Author(s)

T.Koyama, H.Nakayama, K.Nishiyama, N.Takayama.

References

T. Koyama, H. Nakayama, K. Nishiyama, N. Takayama, Holonomic Gradient Descent for the Fisher-Bingham Distribution on the d-dimensional Sphere, Computational Statistics (2013) <http://dx.doi.org/10.1007/s00180-013-0456-z>

See Also

`optim`

Examples

```
## =====
## Example 1. Asteroid data in [N30ST2]
## =====
## Not run:
d <- 2
ss <- c(0.3119,0.0292,0.0707,
        0.3605,0.0462,
        0.3276,
        0.0063,0.0054,0.0762)
start <- c(0.1,0.1,1,1,1,-1,-1,-1,-1)
hgm.z.mleFBBByOptim(d=d,ss=ss,start=start)

## End(Not run)
```

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