## Ramsey Theory in the Multiplicative Integers and Diophantine Approximation

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We shall start with discussing some recent Ramsey-theoretical results in multiplicative integers. These results bring to life some interesting notions of largeness which, in turn, lead to new results related to Diophantine approximations and uniform distribution. We will also discuss some natural open problems and conjectures.