

pfpcoh (cohomology/homology groups for $p \nmid q$)

Edition : auto generated by oxgentexi on 1 June 2016

1 pF_q に関する (コ) ホモロジー

この節では超幾何関数 pF_q (${}_pF_q$) の (コ) ホモロジー群に関連した不変量を計算する関数を解説する.

OpenXM/Risa/Asir での利用にあたっては,

```
load("pfpcoh.rr")$ load("pfphom.rr")$
```

が始めに必要.

1.0.1 pfp_omega

`pfp_omega(P)`

: It returns the Gauss-Manin connection Ω for the generalized hypergeometric function $P F_{P-1}(aa_1, aa_2, \dots; cc_1, cc_2, \dots; x)$.

Description:

Define a vector valued function Y of which elements are generalized hypergeometric function $f_1=F$ and $f_2=xd f_1/dx$, $f_3=xd f_2/dx$, ... It satisfies $dY/dx=\Omega Y$. Generalized hypergeometric function is defined by the series $p F_{p-1}(aa_1, aa_2, \dots; cc_1, cc_2, \dots; x) = \sum_{k=0, \infty} (aa_1)_k (aa_2)_k \dots / (1)_k (cc_1)_k (cc_2)_k \dots x^k$

Example:

```
pfp_omega(3);
```

1.0.2 pfpcoh_intersection

`pfpcoh_intersection(P)`

: `pfpcoh_intersection(P)` returns an intersection matrix for cocycles associated to the generalized hypergeometric function $p F_{p-1}$.

Description:

This program `pfpcoh.rr` computes an intersection matrix S of cocycles of $p F_{p-1}$ and compares it with the matrix obtained by solving a differential equation for intersection matrix.

Algorithm:

Ohara, Sugiki, Takayama, Quadratic Relations for Generalized Hypergeometric Functions $p F_{p-1}$

Example:

```
load("pfpcoh.rr")$
S=pfpcoh_intersection(3);
```

Author : K.Ohara

1.0.3 pfphom_intersection

`pfphom_intersection(P)`

: intersection matrix of homology cycles.

Description:

Computing intersection matrix of cycles associated to pF_{p-1} . As to the meaning of parameters c_1, c_2, c_3, \dots , see the paper Ohara, Kyushu J. Math. Vol. 51 PP.123.

Algorithm:

Ohara, Sugiki, Takayama, Quadratic Relations for Generalized Hypergeometric Functions pF_{p-1}

Example:

```
SS = pfphom_intersection(3)$
```

You get the intersection matrix of homologies for $3F_2$.

Author : K.Ohara

1.0.4 pfphom_monodromy_pair_kyushu

```
pfphom_monodromy_pair_kyushu(P)
:
```

Description:

It returns the pair of monodromy matrices.

Algorithm:

Ohara, Kyushu J. Math. Vol.51 PP.123 (1997)

Example:

```
MP = pfphom_monodromy_pair_kyushu(3)$
```

You get a pair of monodromy matrices for $3F_2$ standing for two paths encircling 0 and 1.

Index

(Index is nonexistent)

(Index is nonexistent)

Short Contents

| | | |
|---|---------------------------------|---|
| 1 | pF_q に関する (コ) ホモロジー | 1 |
| | Index | 3 |

Table of Contents

| | | |
|--------------|------------------------------|----------|
| 1 | pFq に関する (コ) ホモロジー | 1 |
| 1.0.1 | pf _p _omega | 1 |
| 1.0.2 | pfpcoh_intersection | 1 |
| 1.0.3 | pfphom_intersection | 1 |
| 1.0.4 | pfphom_monodromy_pair_kyushu | 2 |
| Index | | 3 |